

**Consideration of Variability & Uncertainty in
Developing Phosphorus TMDL's
for Lakes & Reservoirs**

William W. Walker, Jr., Ph.D.

Environmental Engineer

Concord, Massachusetts

wwwalker@shore.net

<http://www.shore.net/~wwwalker>

**Workshop: Water Quality Management & Restoration
Using Settling Basins, Wetlands, & Other Watershed BMPs
St. Paul, Minnesota**

July 11, 2001

??? **Total Maximum Daily Load** ???



Iterative TMDL Process

Define Management/Use Objectives

Identify Water Quality Standards

Monitor & Model

Estimate TMDL's

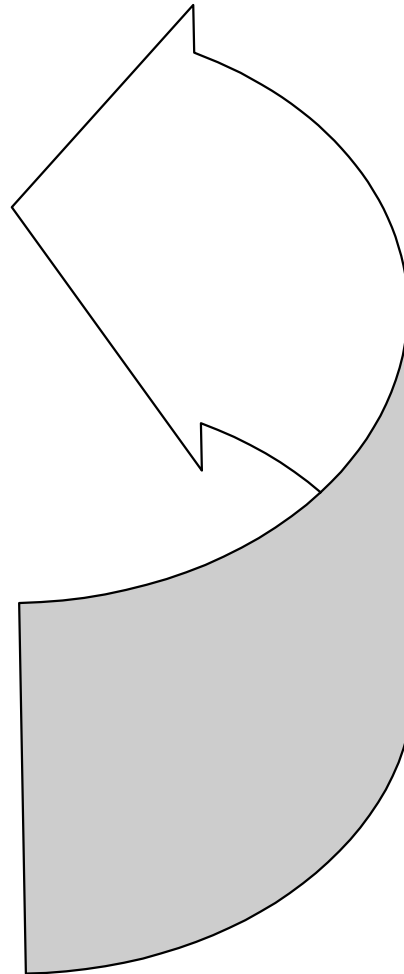
Evaluate Controls

Develop Load Allocations

Implement Controls

Monitor Results

Objectives Achieved ?



~ 5-10 years?

TMDL Equations

Watershed Mass Balance:

$$\text{TMDL} = \Sigma \text{LAs} + \Sigma \text{WLAs} + \text{Background} + \text{MOS}$$

Total Maximum Daily Load = Non-Point Sources + Point Sources + Natural or Unregulated + Margin of Safety

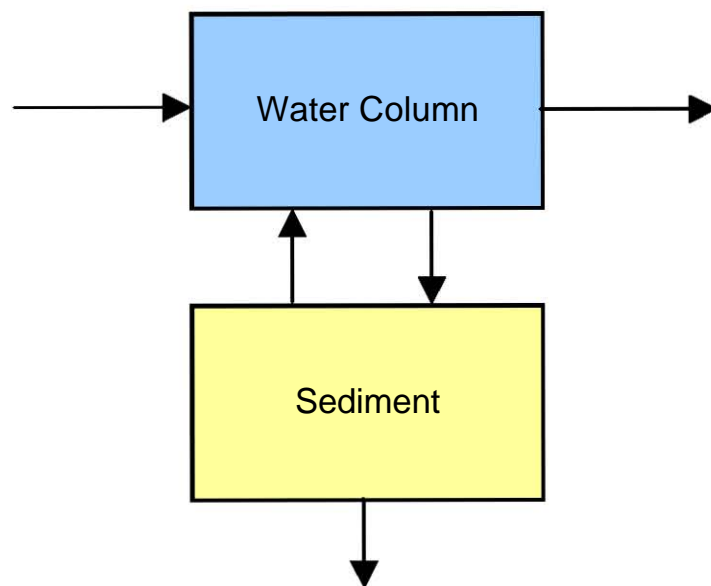
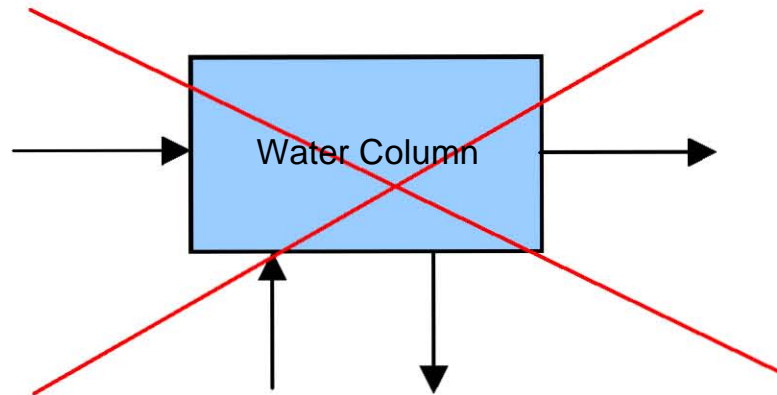
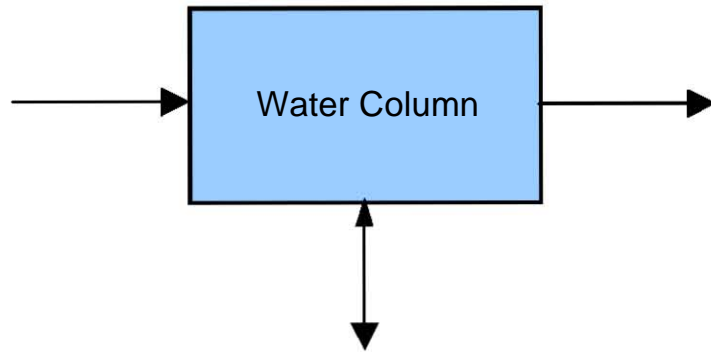
Lake/Reservoir Mass Balance:

$$\text{TMDL} = Q_0 P^* + K_{\text{NET}} A P^* + L_i$$

Input = Flushing + Net Retention + "Internal Load"



Alternative Mass Balance Models



Quantifying Variability & Uncertainty Benefits

Provides Realistic Assessment

Provides Rational Basis for MOS

Helps to Define Lake Goal

Numerical Value "Target" or "Limit"?

Spatial & Temporal Averaging

Compliance Rate

Identifies Important Sources of Uncertainty

Provides Incentive for Continued Data Collection & Modeling

More Data --?-> Lower MOS --?--> Higher Load Alloc

Increases Probability of Success

Quantifying Variability & Uncertainty Difficulties

Vague & Difficult Concepts

Limited Guidance Provided in TMDL Regulations

Frequency Concepts Rarely Built into WQ Standards

Load Allocations Sensitive to Assumptions:

Compliance Rate (e.g., % of yrs \leq target)

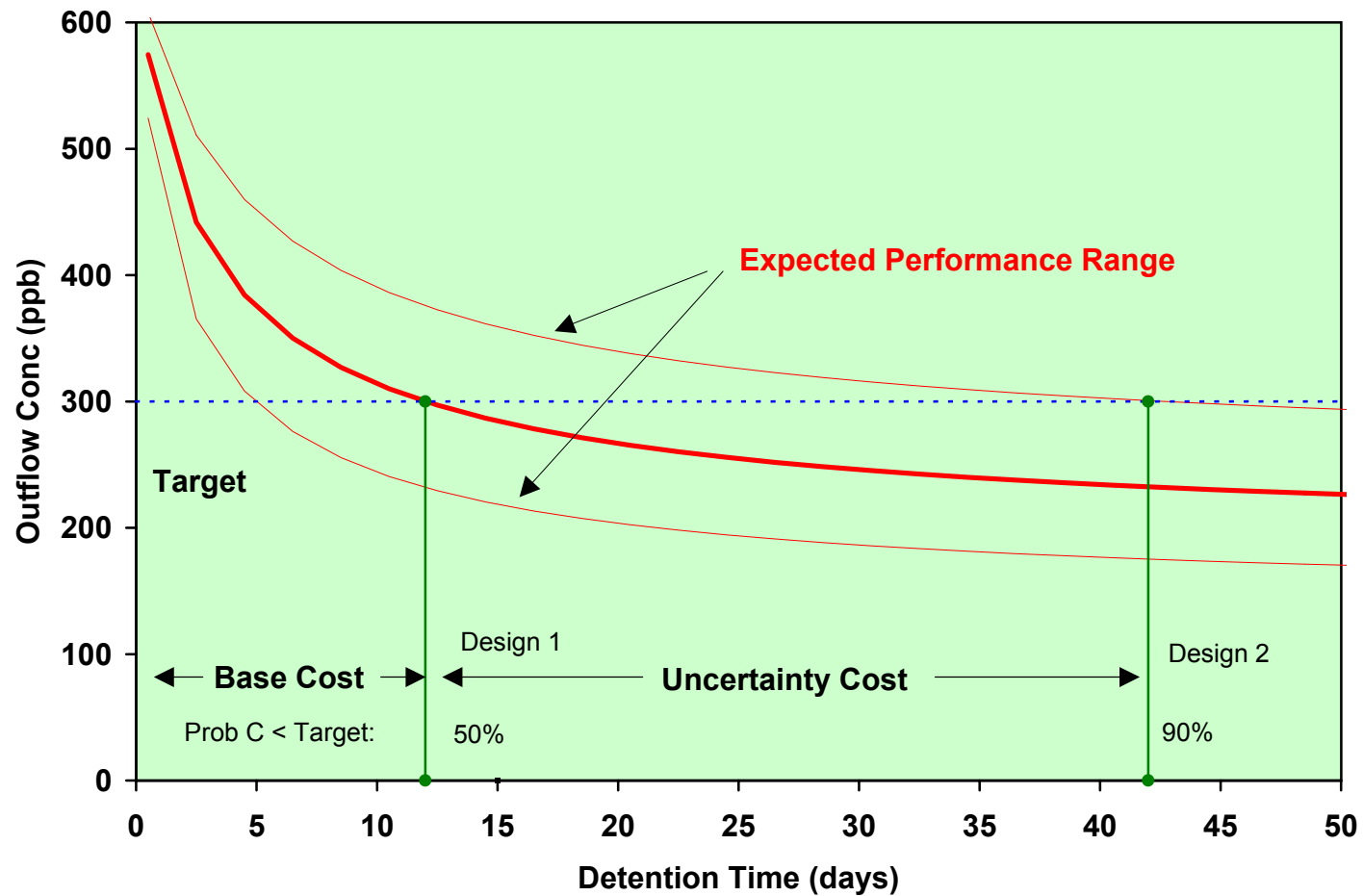
Confidence Level (~probability of success)

Uncertainty Costs (MOS) Can Be Large

Can Backfire & Retard Restoration Efforts

Uncertainty Estimates are Uncertain

Potential Uncertainty Costs in Detention Basin Design



Modeling Variability & Uncertainty Stochastic Approach

Expected Long-Term Average Mass-Balance:

$$P_M = L_M / (K_{NET} + Q_S)$$

Accounting for Uncertainty:

$$P_{MU} = P_M \exp(d_u)$$

d_u = random error term, mean = 0, std dev = s_u

$$s_u \sim 0.1 - 0.5$$

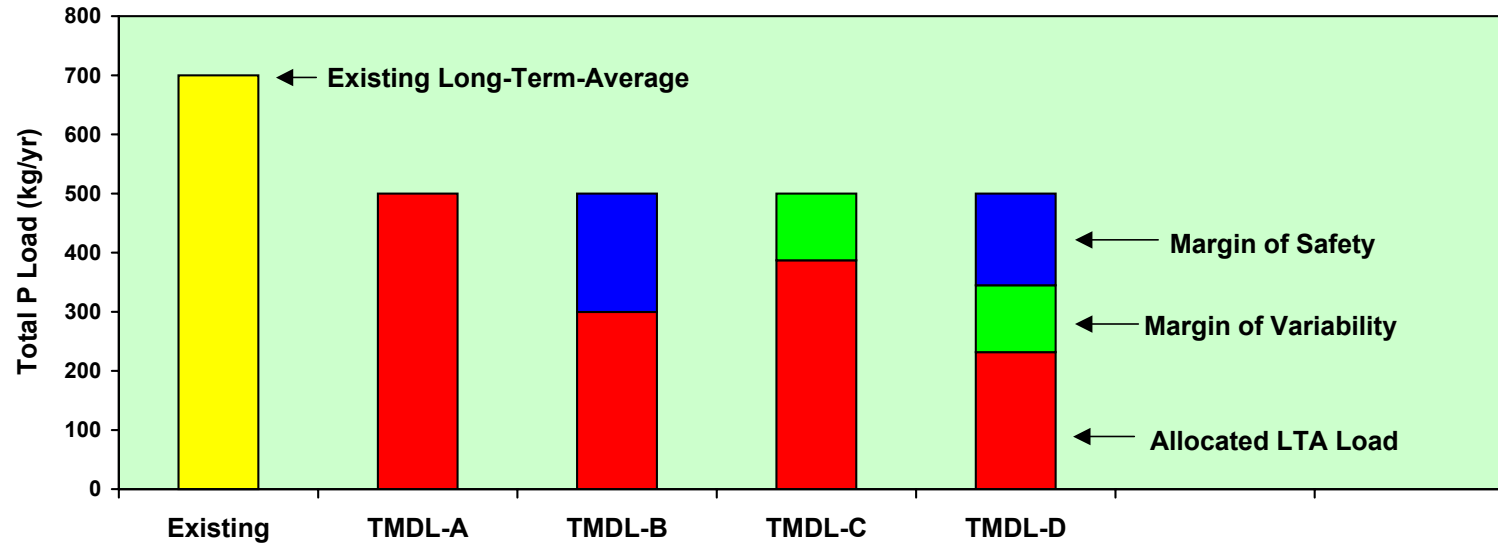
Accounting for Uncertainty & Variability:

$$P_{MUY} = P_M \exp(d_u + d_y)$$

d_y = random yr-to-yr variation, mean = 0, std dev = s_y

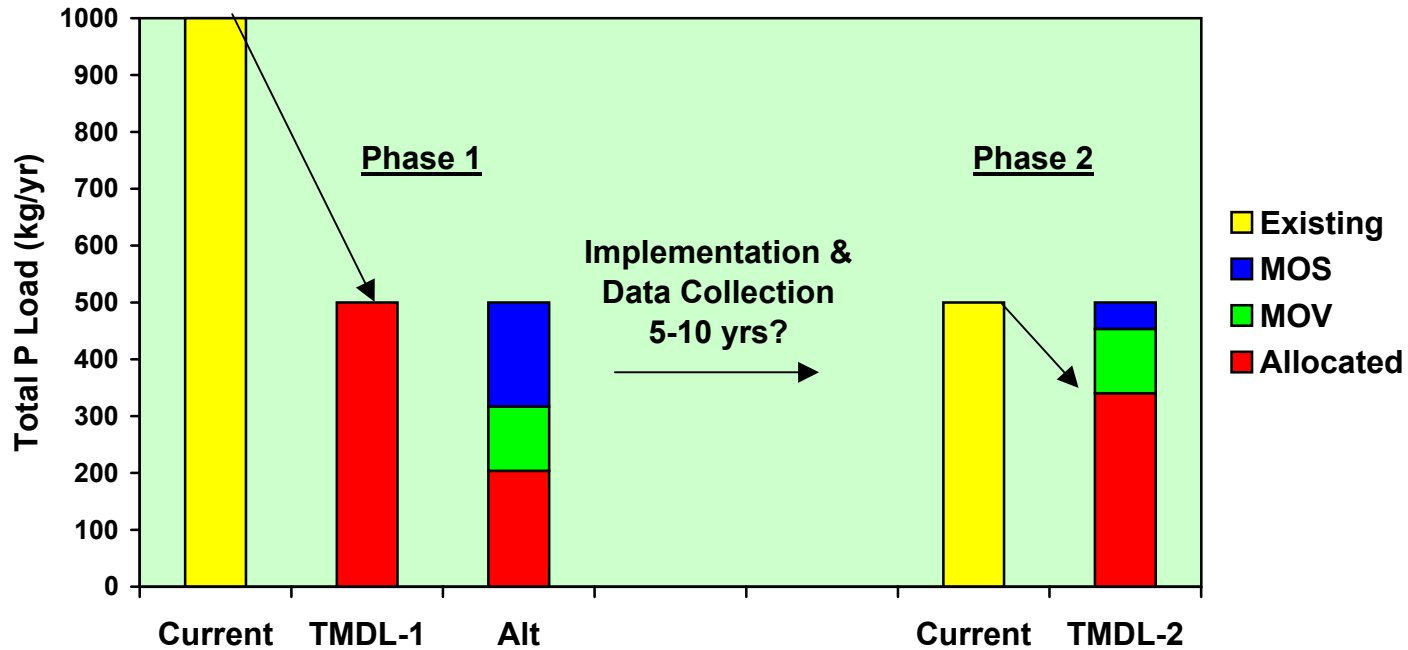
$$s_y \sim 0.1 - 0.3$$

Alternative TMDL Formulations



Lake P Target	<u>LT-Avg</u>	<u>LT-Avg</u>	<u>10-Yr Max</u>	<u>10-Yr Max</u>
Uncertainty Considered	No	Yes	No	Yes
Variability Considered	No	No	Yes	Yes
Confidence Level --->MOS	50%	90%	50%	90%
Compliance Freq --> MOV	50%	50%	90%	90%
Model Error Std Dev	0.4	0.4	0.4	0.4
Temporal Std Dev	0.2	0.2	0.2	0.2
Allocated Load	500	299	387	232
Load Reduction	29%	57%	45%	67%
Uncertainty Cost		29%		22%

Phased Approach to TMDL Implementation



Confidence Level	50%	90%		90%
Compliance Freq	50%	90%	Uncertainty Reduction	90%
Model Error Std Dev	0.5	0.5		0.1
Temporal Std Dev	0.2	0.2		0.2
Allocated Load	500	204		340
Load Reduction	50%	80%		66%

- TMDL = Allocated Long-Term Average Load + MOV + MOS
- MOV = Margin of Variability
- MOS = Margin of Safety

Including a Margin of Safety in TMDL's

Conservative Water Quality Criteria/Standard

Conservative Phosphorus Goal

Conservative Modeling Assumptions

Conservative Effluent Limits / Discharge Permits

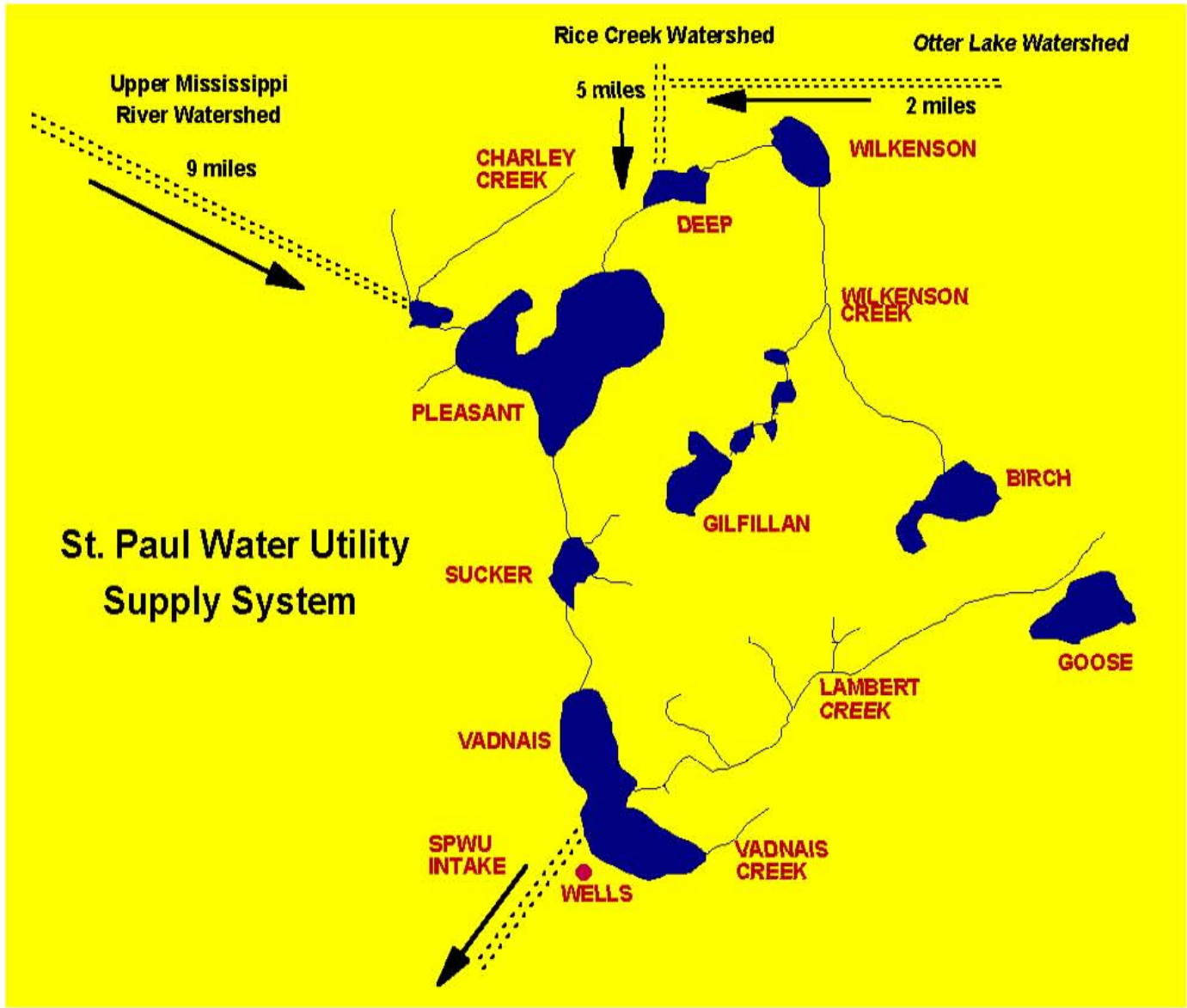
Conservative Facility Designs

Conservative Growth Projections

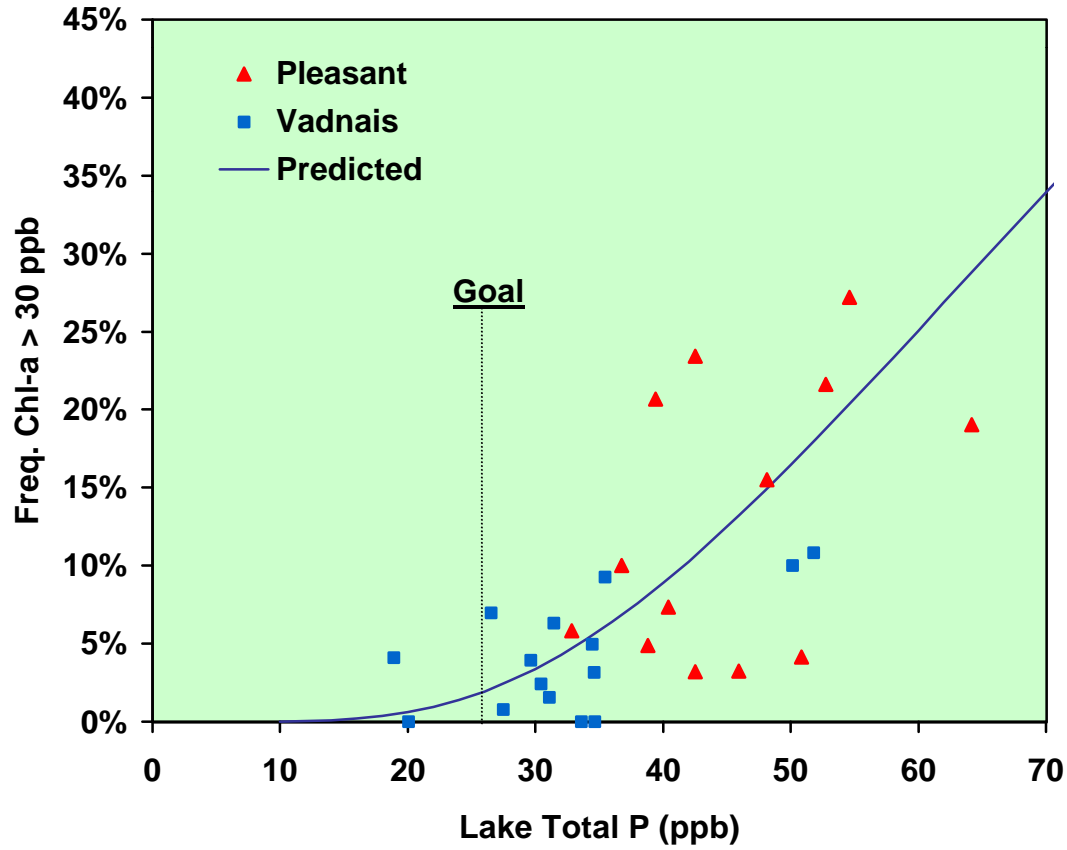
Shell Game

Examples of Phosphorus TMDL's & Similar Control Programs

<u>Lake/Reservoir</u>	<u>Klamath</u>	<u>Cherry Creek</u>	<u>Vadnais</u>	<u>Onondaga</u>	<u>Okeechobee</u>	<u>Everglades Phase I</u>	<u>Everglades Phase II</u>
State	Oregon	Colorado	Minnesota	New York	Florida	Florida	Florida
Concern	pH, Blooms, DO	Blooms	Taste & Odor	Blooms, Transparency	Blooms	Ecosystem Imbalance	Ecosystem Imbalance
Numerical Criterion	pH < 9	Chl-a < 15 ppb	Chla < 20 ppb	Secchi > 4 ft	Chla < 40 ppb	Tech-Based	TP < 10 ppb
Time Scale	Daily	Summer	Daily	Daily	Daily	Long-Term	Long-Term
Compliance Rate	90%	90%	90%	?	90%	50%	50%
P Balance Model	Dynamic	Dynamic	Steady State	Steady-State	Dynamic	Steady-State	Dynamic
Phosphorus Goal	Spring	Summer	Summer	Summer	Long-Term	Long-Term Flow-Wtd	Long-Term Geometric
Historical P (ppb)	60	60	60	58	87	170	50
Target P (ppb)	20	35	25	20	40	50	10
Conc Reduction	67%	42%	58%	66%	54%	71%	80%
Other Factors	Background		Treatment Costs	State P Criterion		Technology-Based	Background

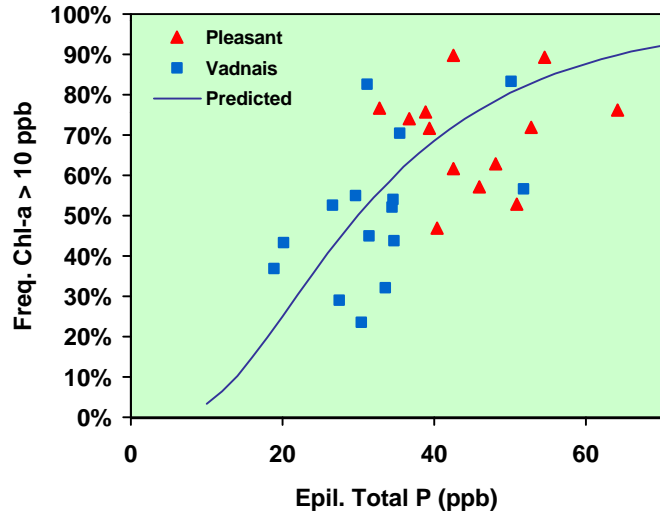


Algal Bloom Frequency vs. Total Phosphorus



Bloom Frequencies from daily samples at Vadnais Intake & Pleasant Gatehouse
Total Phosphorus concentrations measured in Lake Epilimnion (0- 6 m)
April-September Means for Each Year

Algal Bloom Frequencies vs. Total Phosphorus



Model:

$$B_a = k P$$

$$B_g = B_a / \exp(S^2 / 2)$$

$$Z^* = \ln(B^* / B_g) / S$$

$$\text{Freq}(B > B^*) = 1 - \text{NORMSDIST}(Z^*)$$

Coefficients:

$$k = 0.4$$

$$S = 0.6$$

Variables:

P = april-sept. epilimnetic mean total p (ppb)

B_a = arithmetic mean chl-a (ppb)

B_g = geometric mean chl-a (ppb)

B^* = bloom criterion (ppb)

S = standard deviation of $\ln(\text{Chl-a})$

Z^* = standard normal deviate

NORMSDIST = cumulative normal distrib. (Excel)

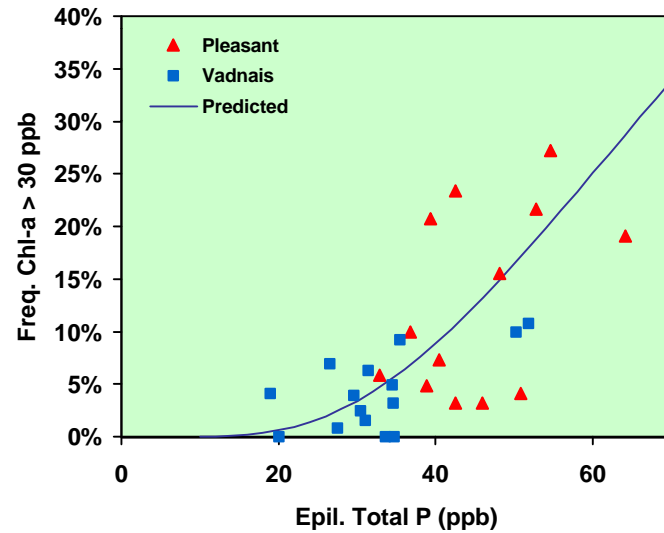
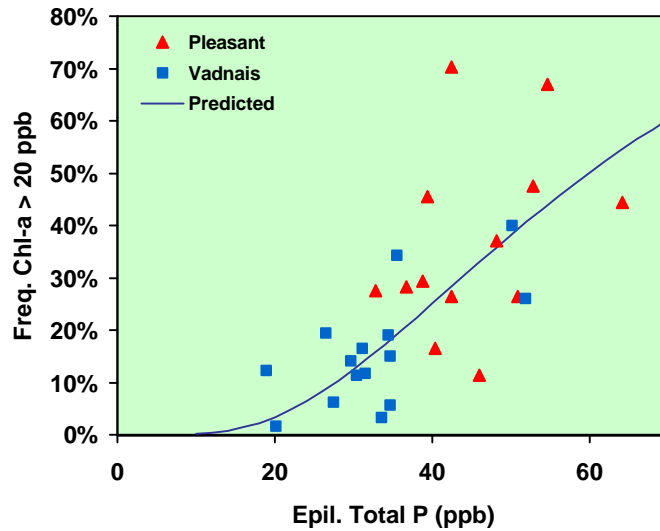
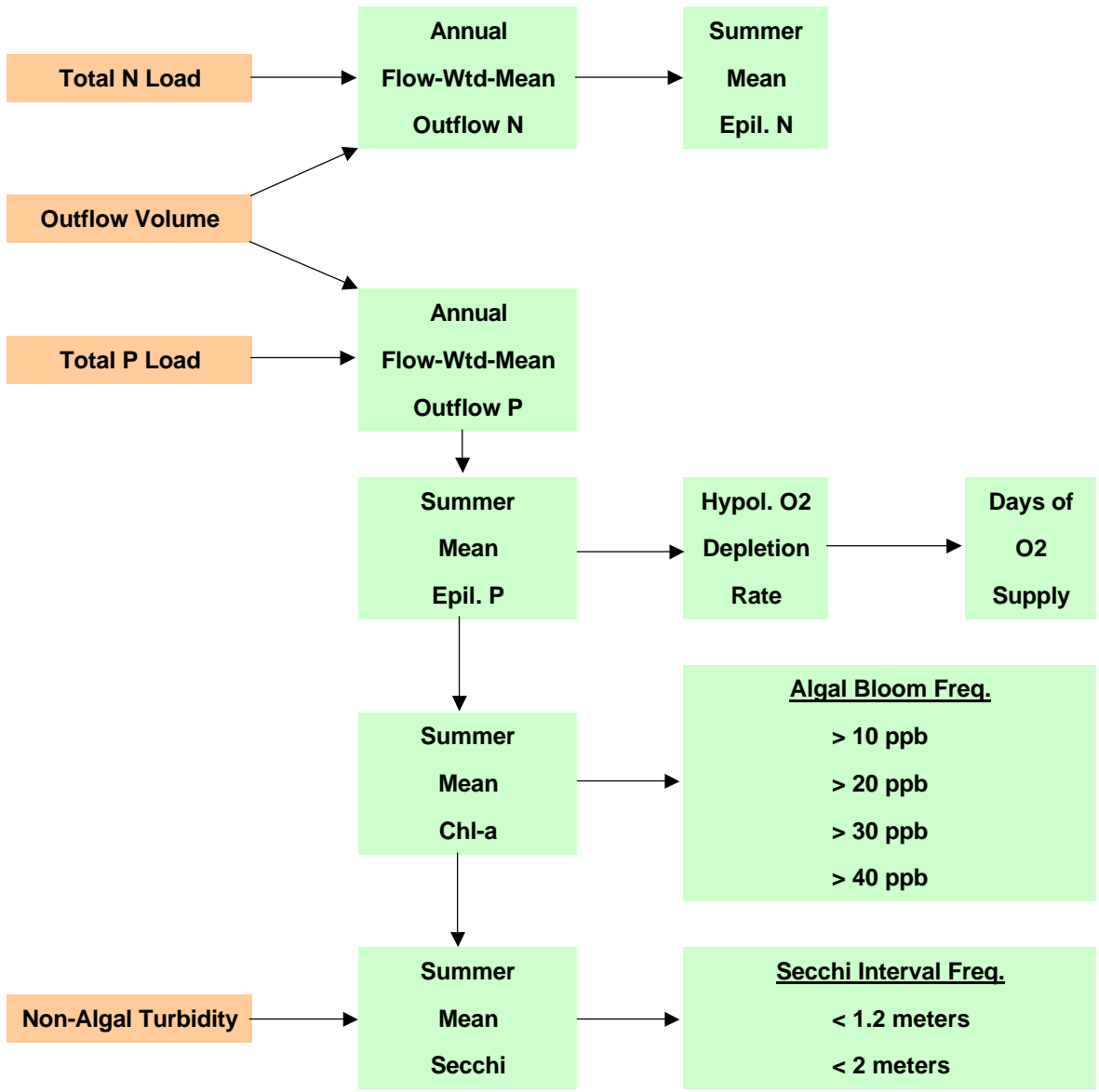
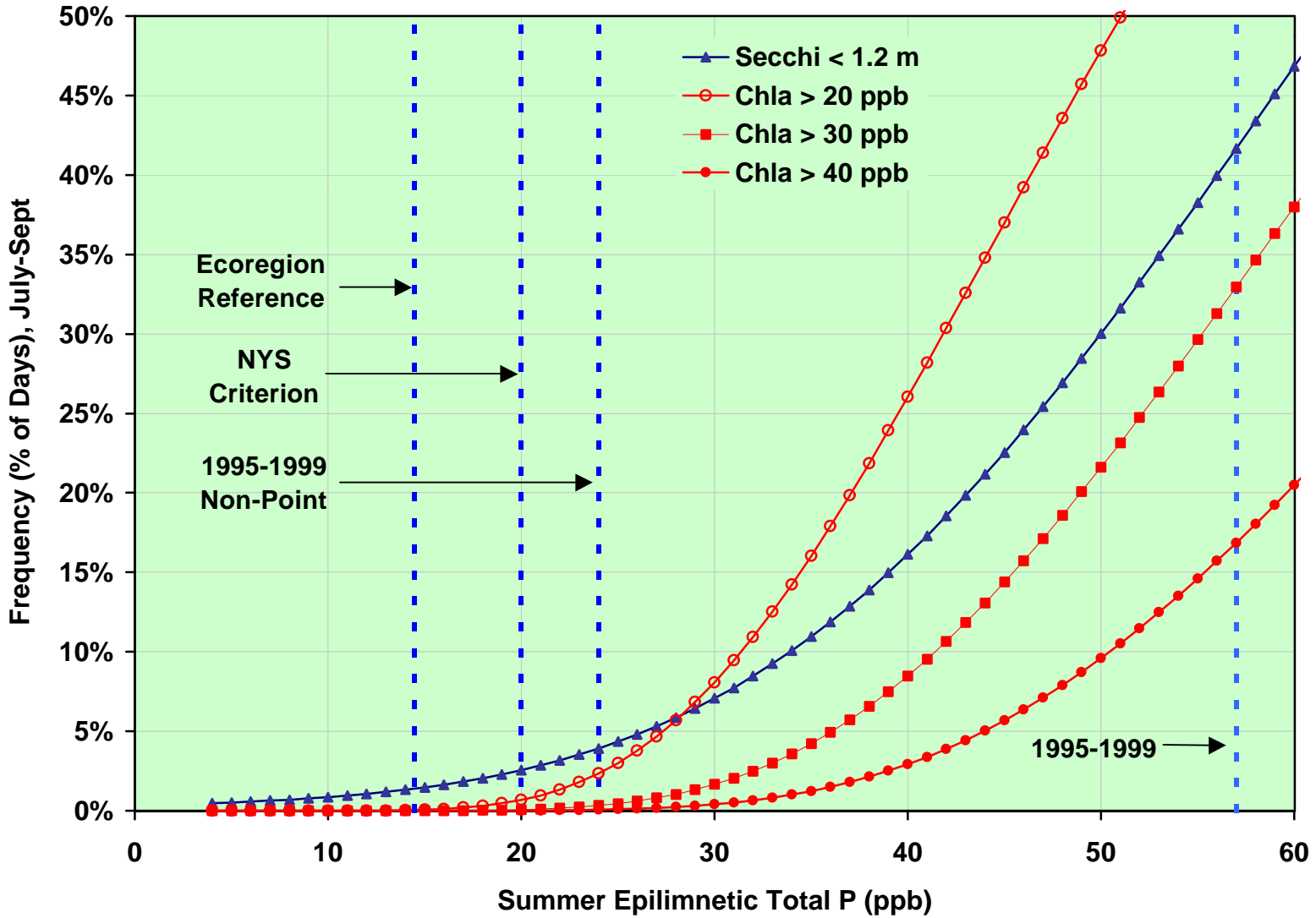


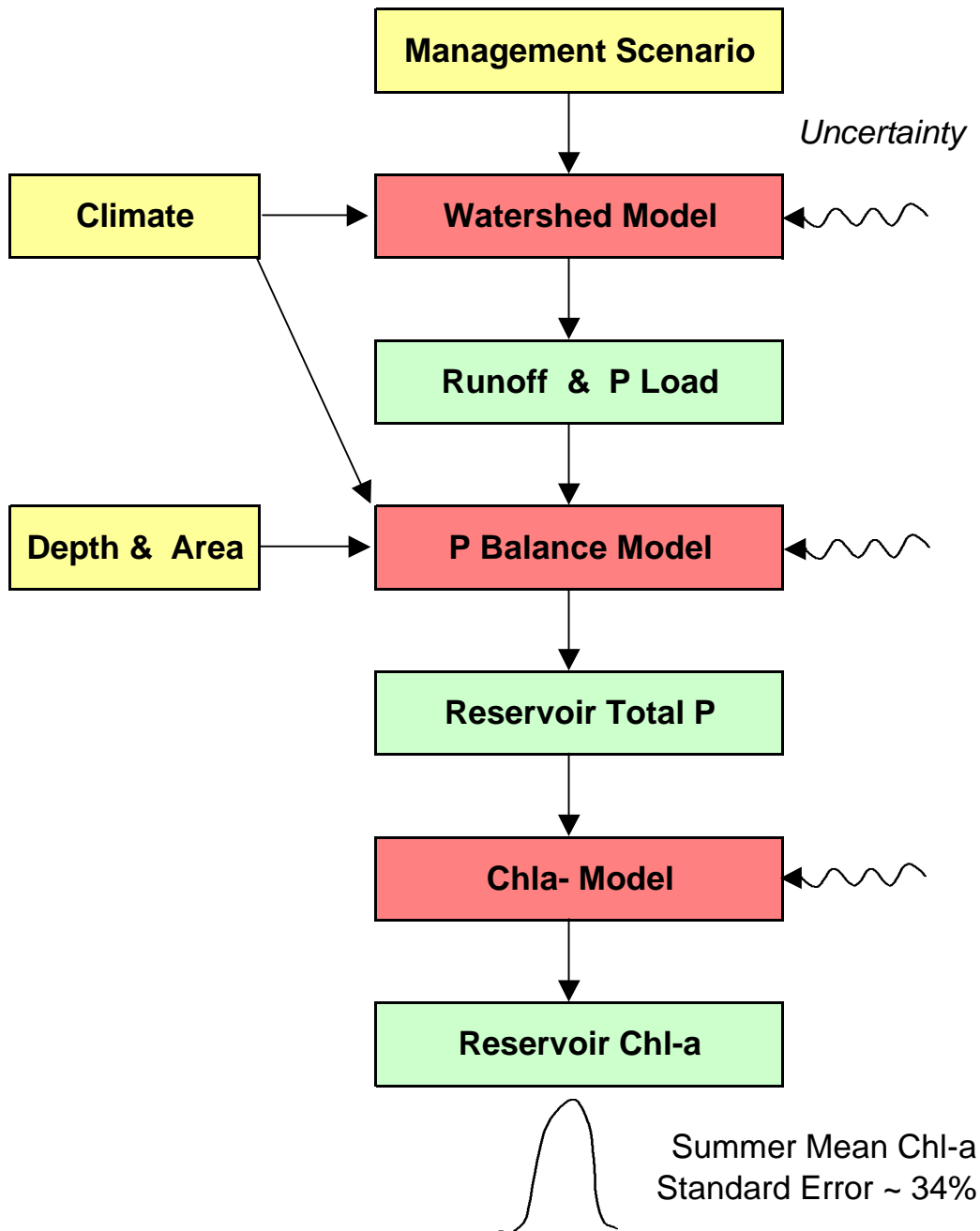
Figure 12-2
Eutrophication Model Network for Onondaga Lake



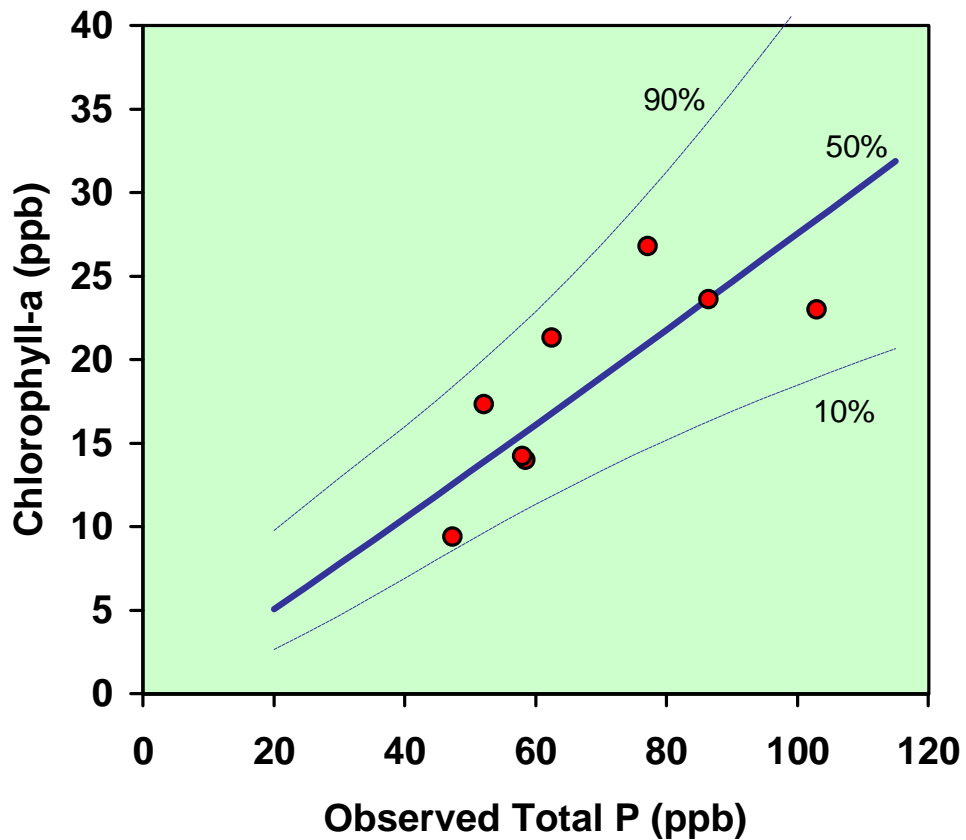
Phosphorus Criteria for Onondaga Lake



Linkage of Models Used to Forecast Reservoir Chlorophyll-a Levels



Prediction Intervals for Chlorophyll-a based upon Observed Total P



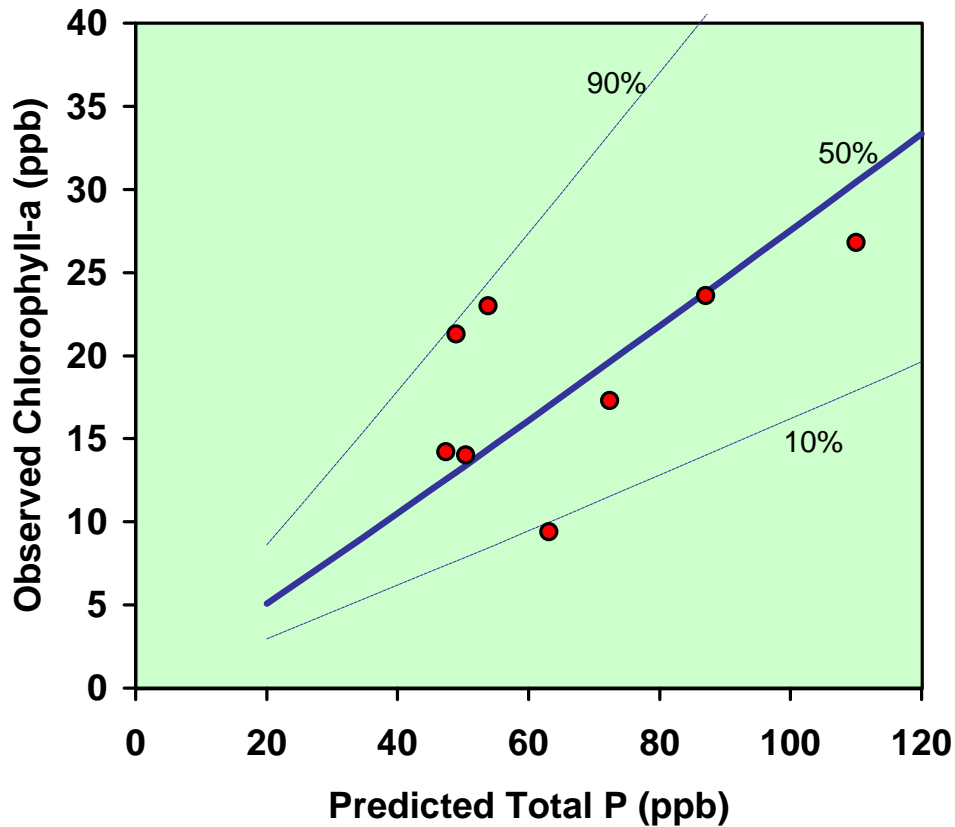
Symbols = Measured July-Sept.mean Chl-a, 1992-1999

X- Axis = Observed July-Sept mean Total P

Lines = Chl-a prediction interval using regression model

Residual Standard Error = 23%

Prediction Intervals for Chlorophyll-a using Coupled Mass-Balance & Regression Models



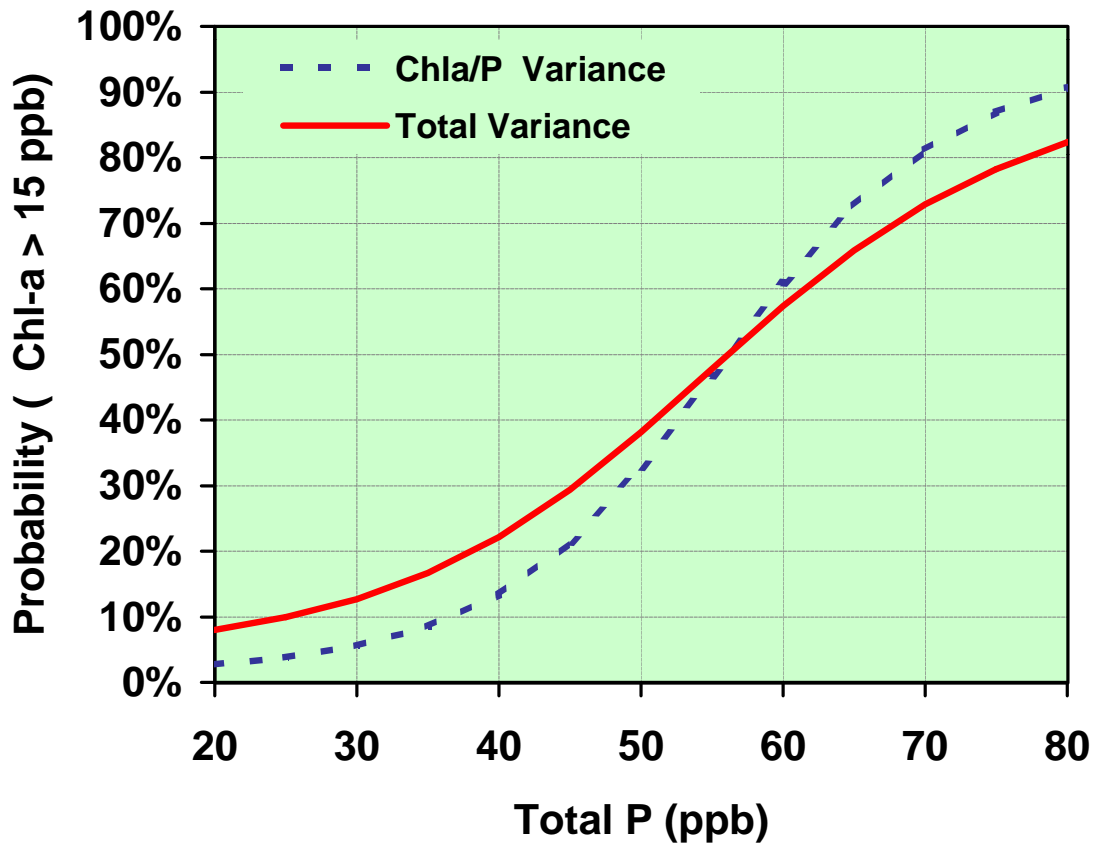
Symbols = Measured July-Sept. Mean Chl-a, 1992-1999

X- Axis = Total P predicted from mass-balance model
used in TMDL analysis (Appendix K, Table 2)

Predicted = Chl-a predicted from coupled mass-balance &
Chl-a vs. TP regression models

Residual Standard Error = 38%

Risk of Exceeding 15 ppb Chl-a vs. Total P in Any Year



Y-Axis: Probability (July-Sept. Mean Chl-a > 15 ppb)

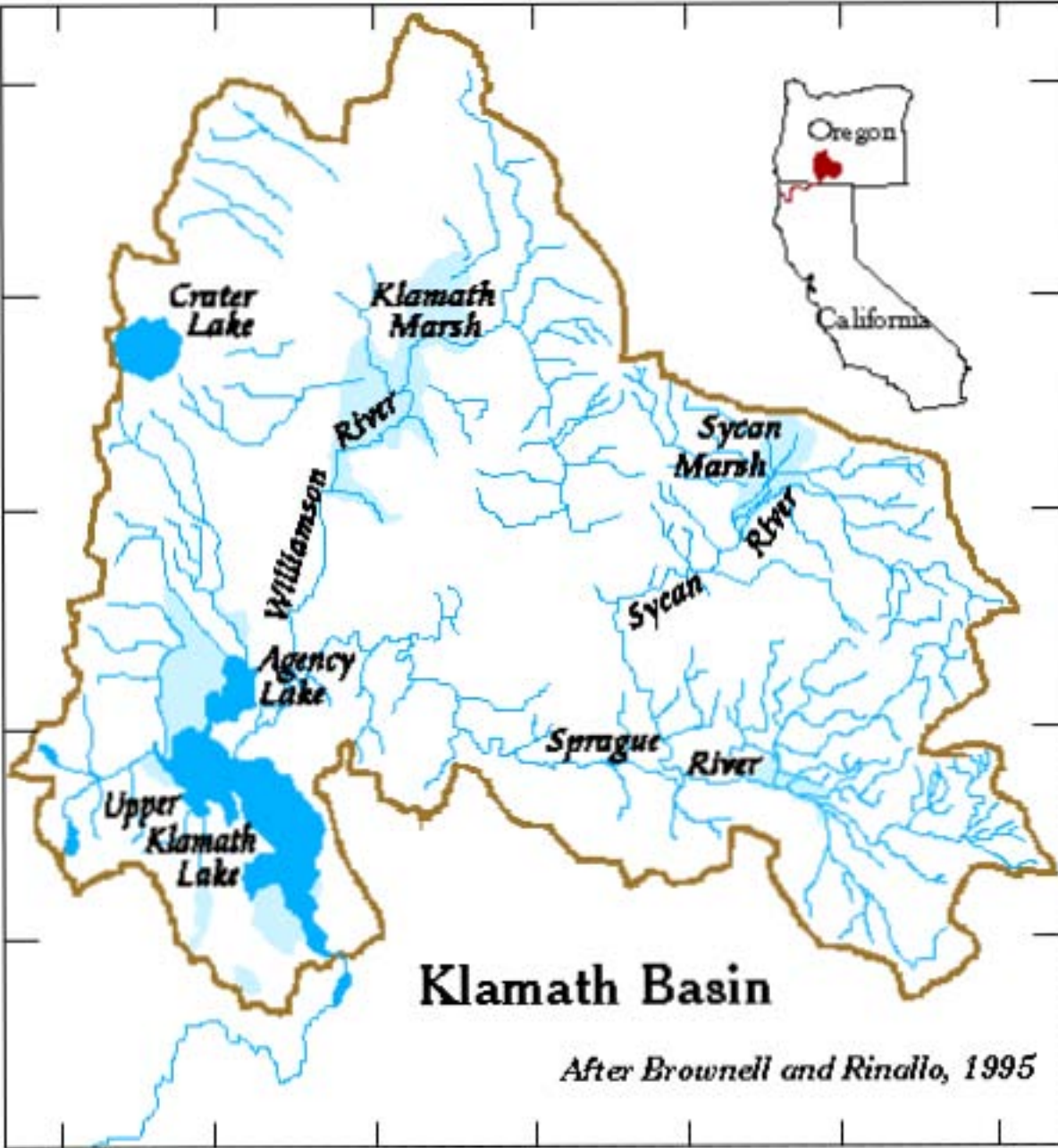
Uncertainty Sources:

Chl-a/P	Chlorophyll-a vs. Total P Regression
Total	Coupled Mass-Balance Model & Chl-a vs. TP Regression

X-Axis: July-Sept Mean Total P

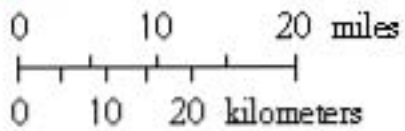
15" 122'00" 45" 30" 15" 121'00" 120'45"

15"
43'00"
45"
30"
15"
42'00"



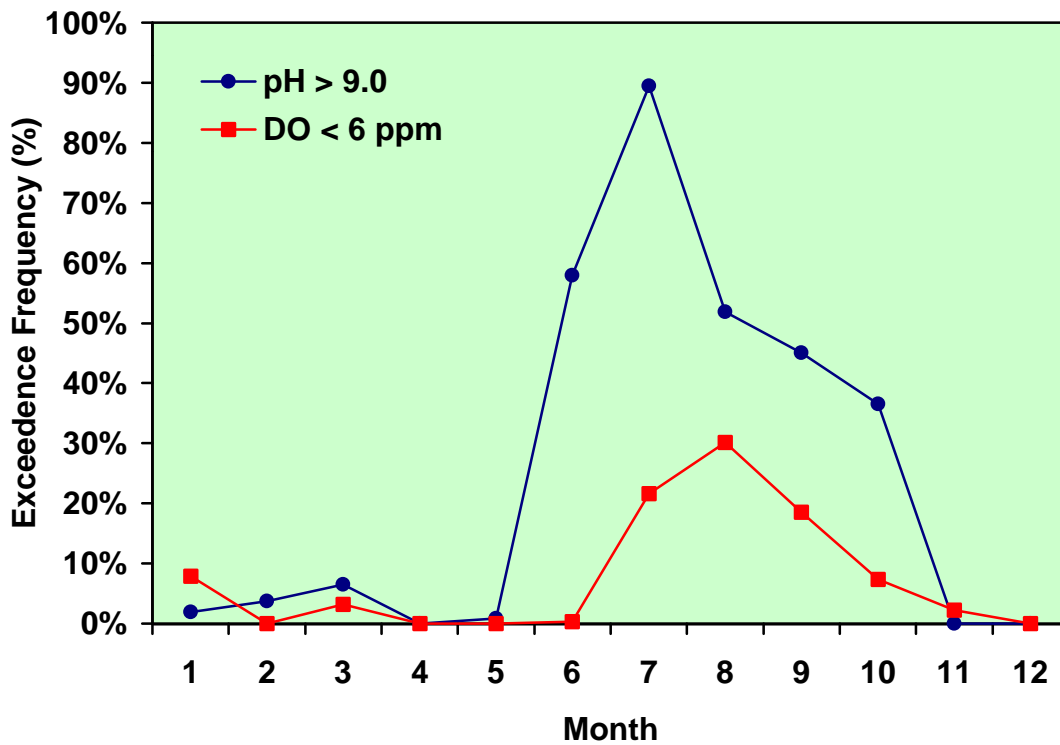
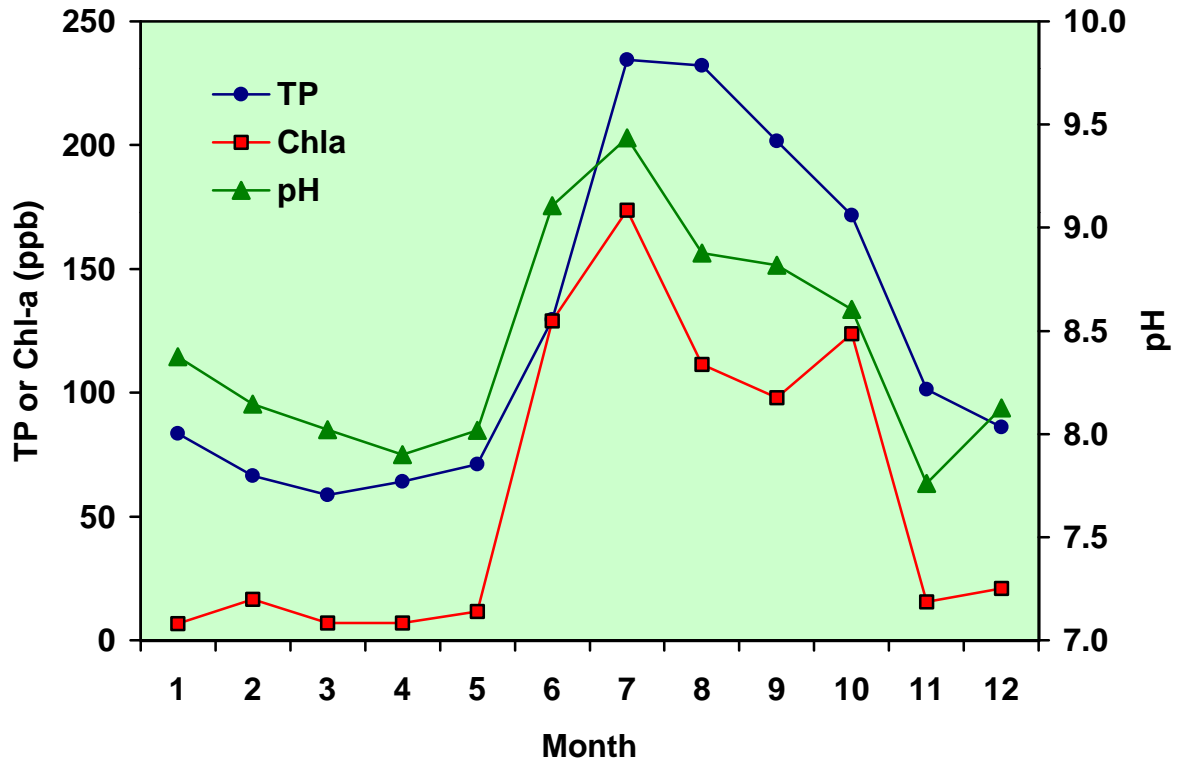
Klamath Basin

After Brownell and Rinallo, 1995

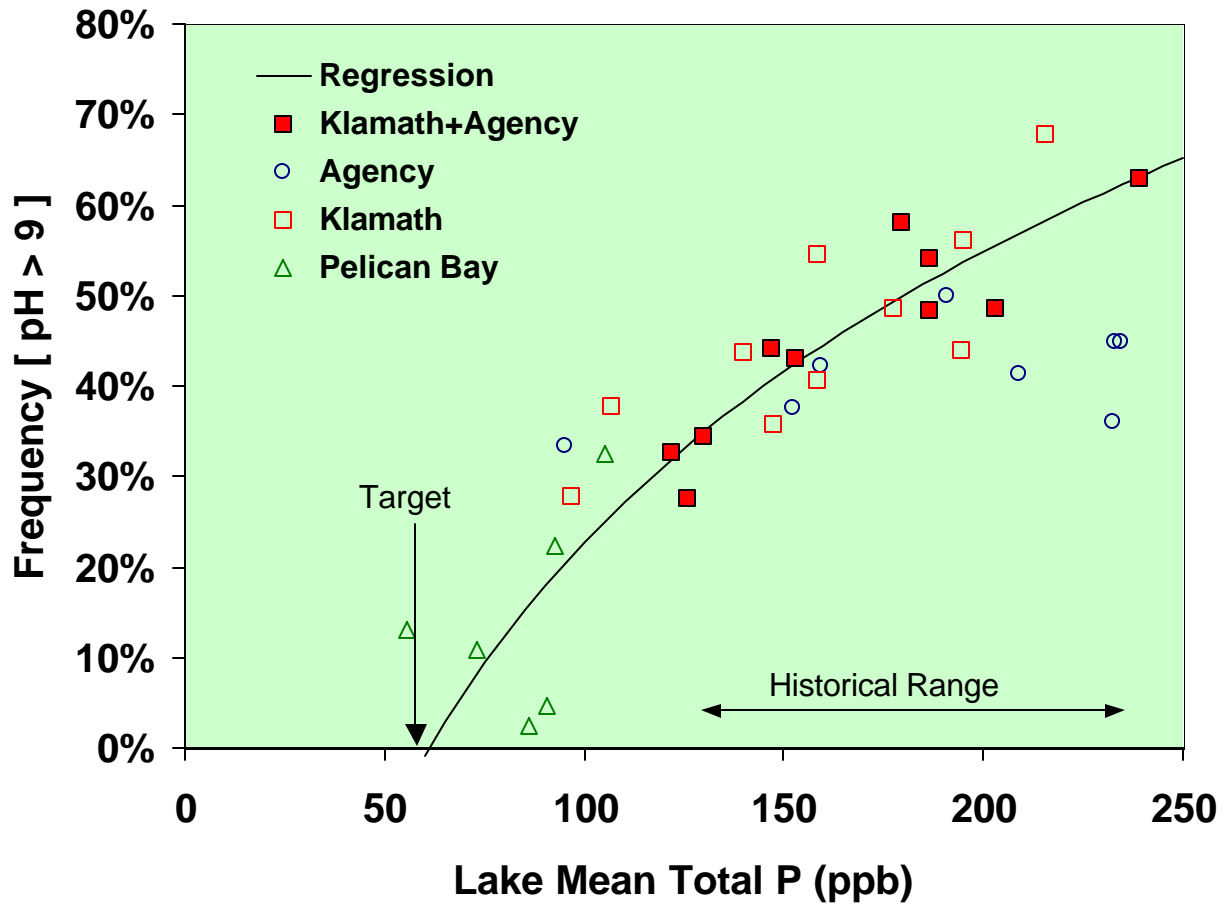


*S.M. Colman and J.S. Hatton
U.S. Geological Survey*

Seasonal Variations - Upper Klamath Lake



Derivation of Phosphorus Target for Upper Klamath Lake for Compliance with pH Standard



Yearly Means by Lake Region, April-October
 Frequency = % of Measurements (All Stations & Depths) Exceeding pH 9

DRAFT

Figure 11
Model Structure

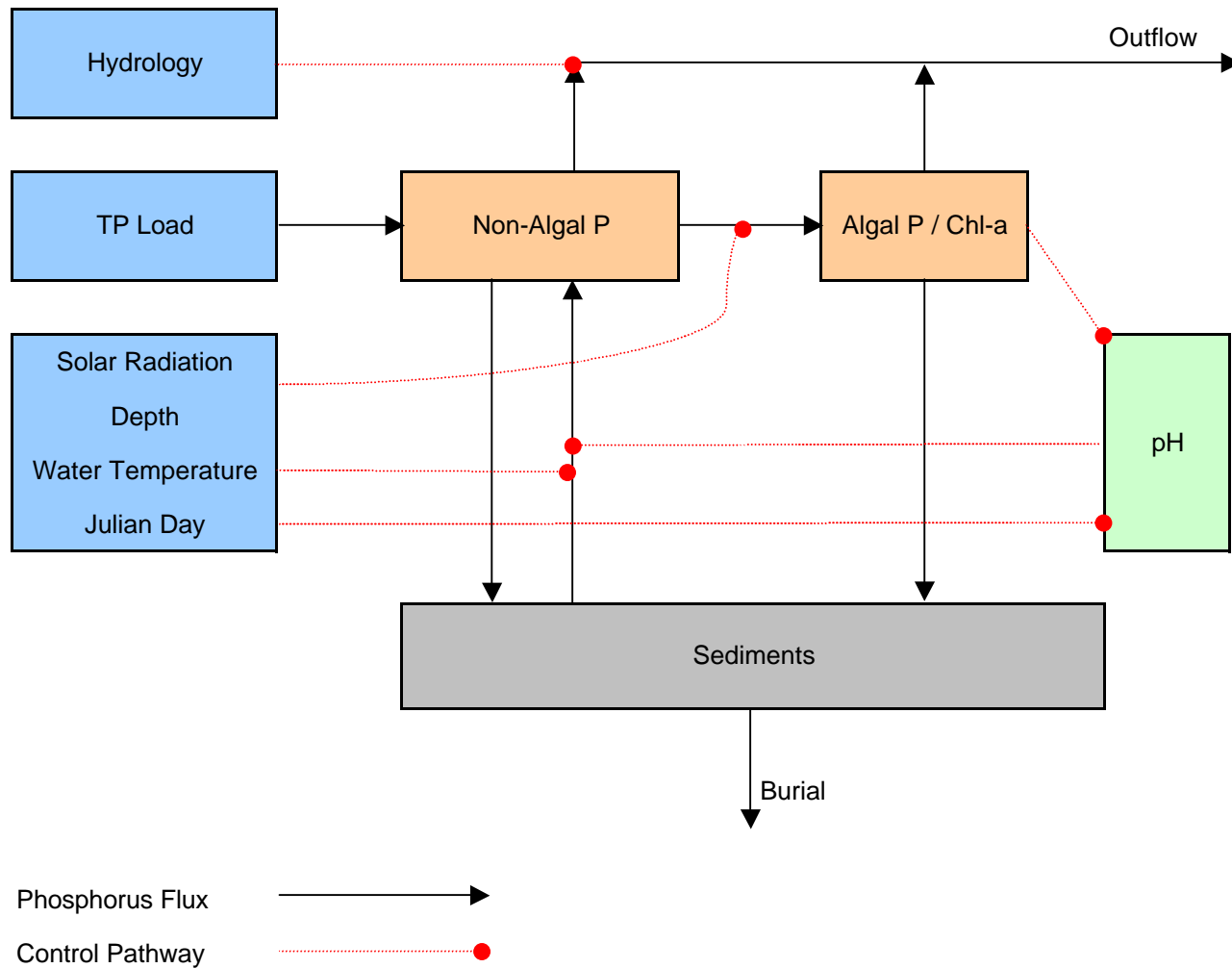
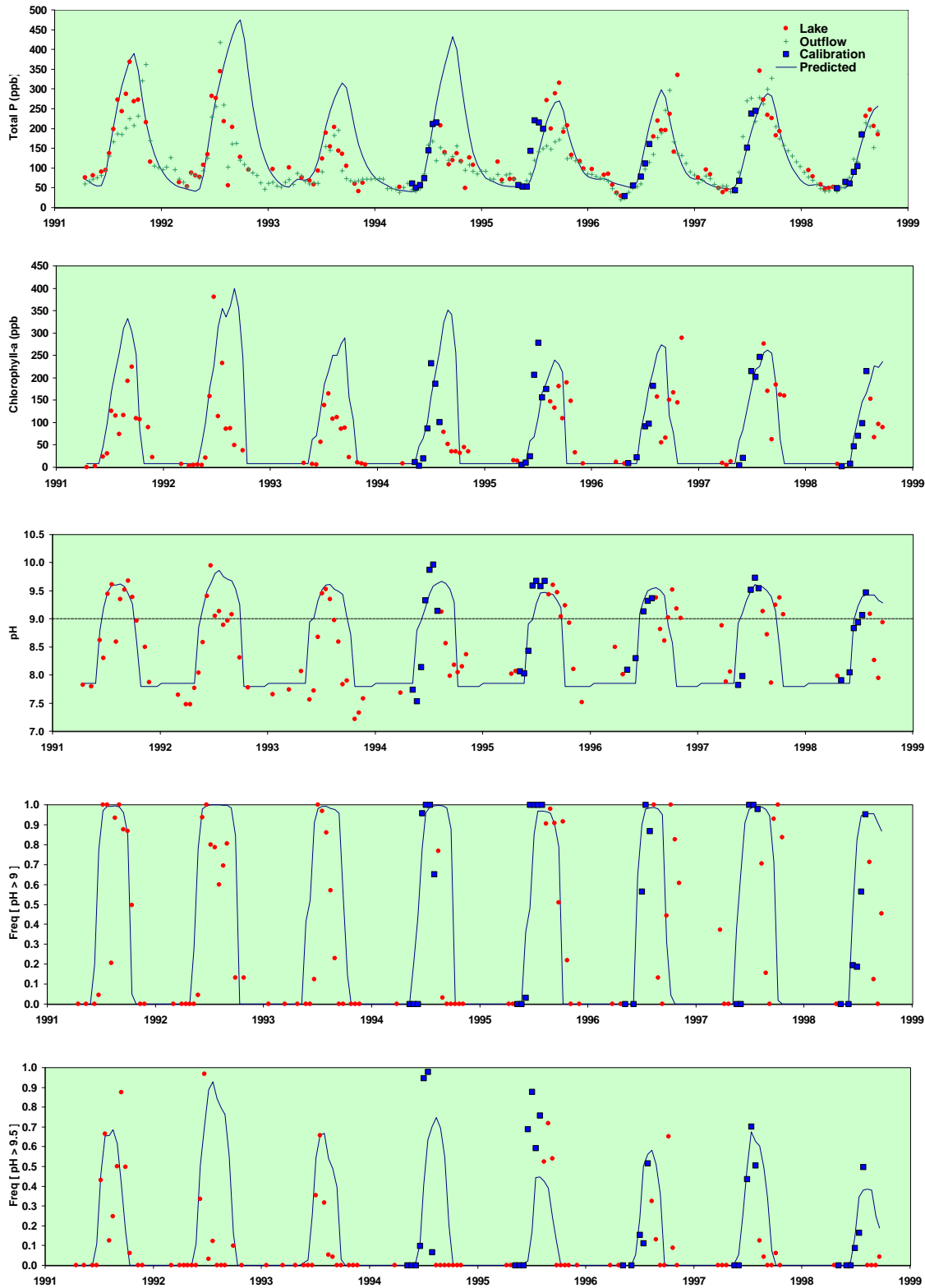
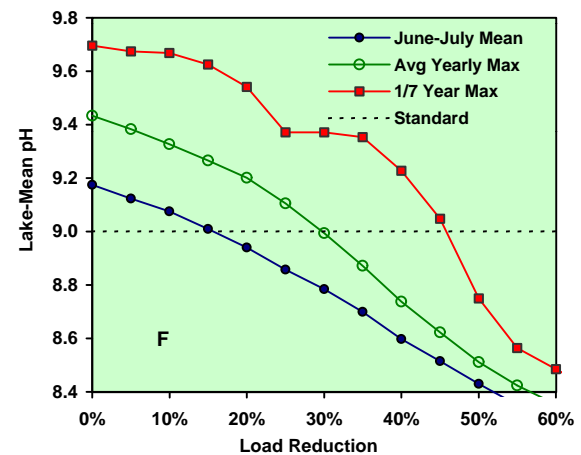
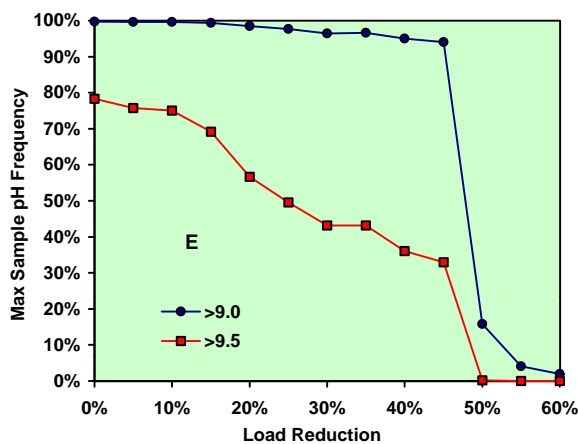
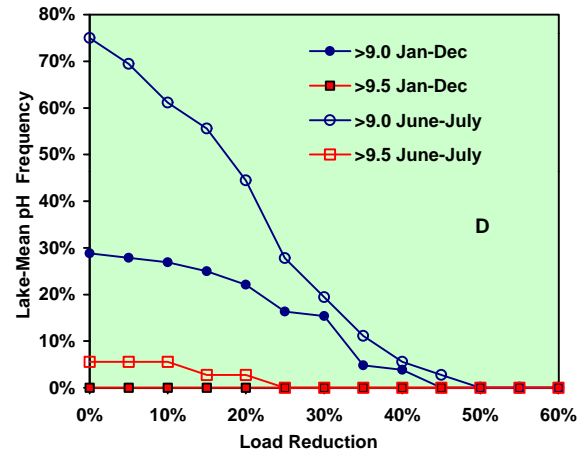
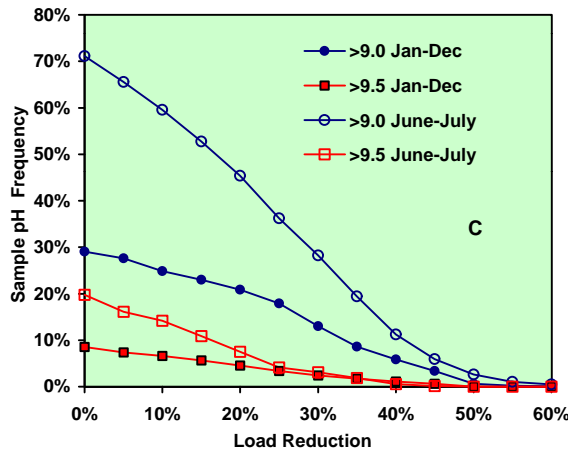
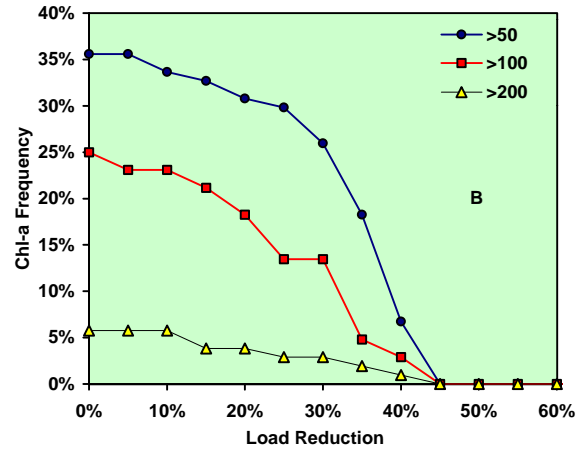
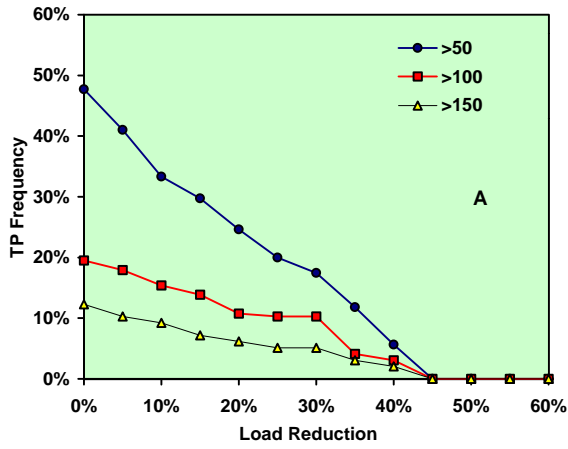


Figure 20
Observed & Predicted Time Series Driven by Phosphorus Loads



Top: Observed Lake P & Outlet P concentrations
 Lines: TP, Chl-a, pH, & pH Frequency predicted from external P loads & other controlling factors (light, temp., depth, flushing, etc.)
 Squares: Observed values used for model calibration (May-July, 1994-1999)
 Circles: Observed values used for model testing

Figure 24
Excursion Frequencies vs. Phosphorus Load Reduction



A,B: Total P & Chl-a Frequencies for January-December, Averaged over 7 Years

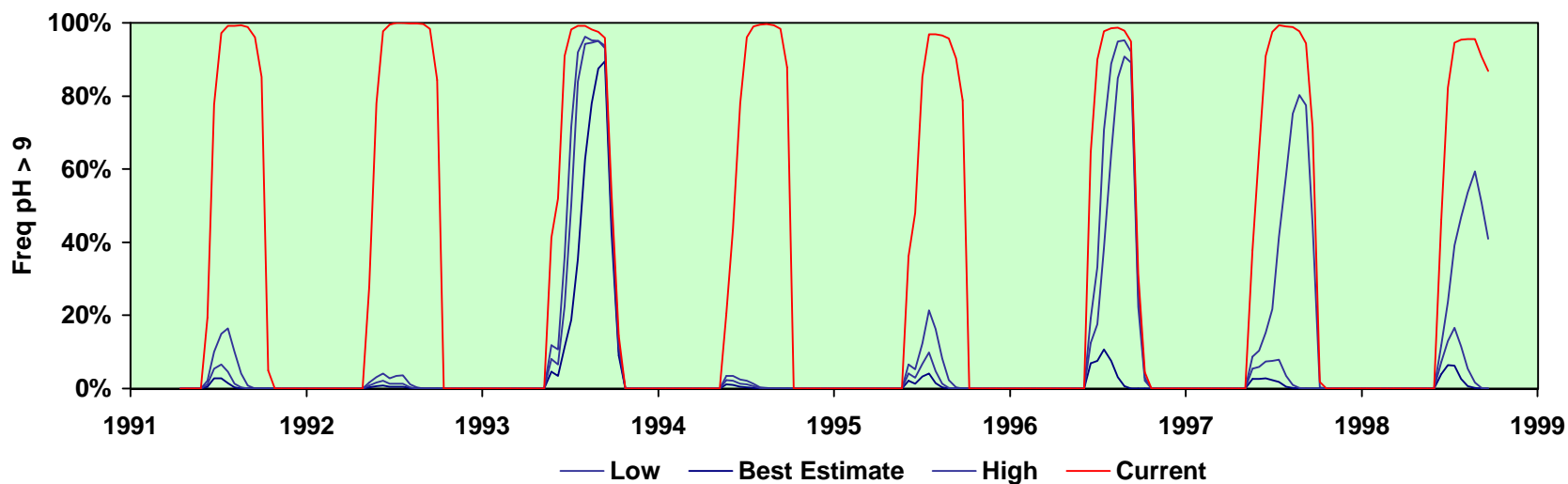
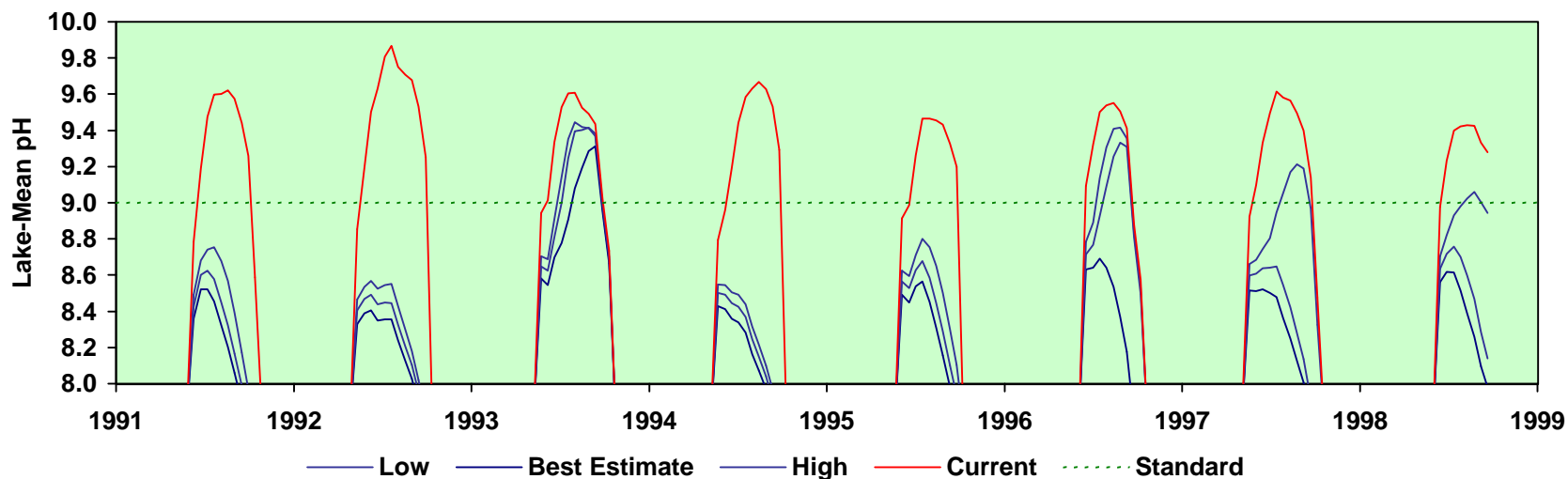
C: % of pH Measurements, Averaged Over 7 Years, For Jan-Dec & June-July

D: % of Lake-Mean pH Values, Averaged Over 7 Years, For Jan-Dec & June-July

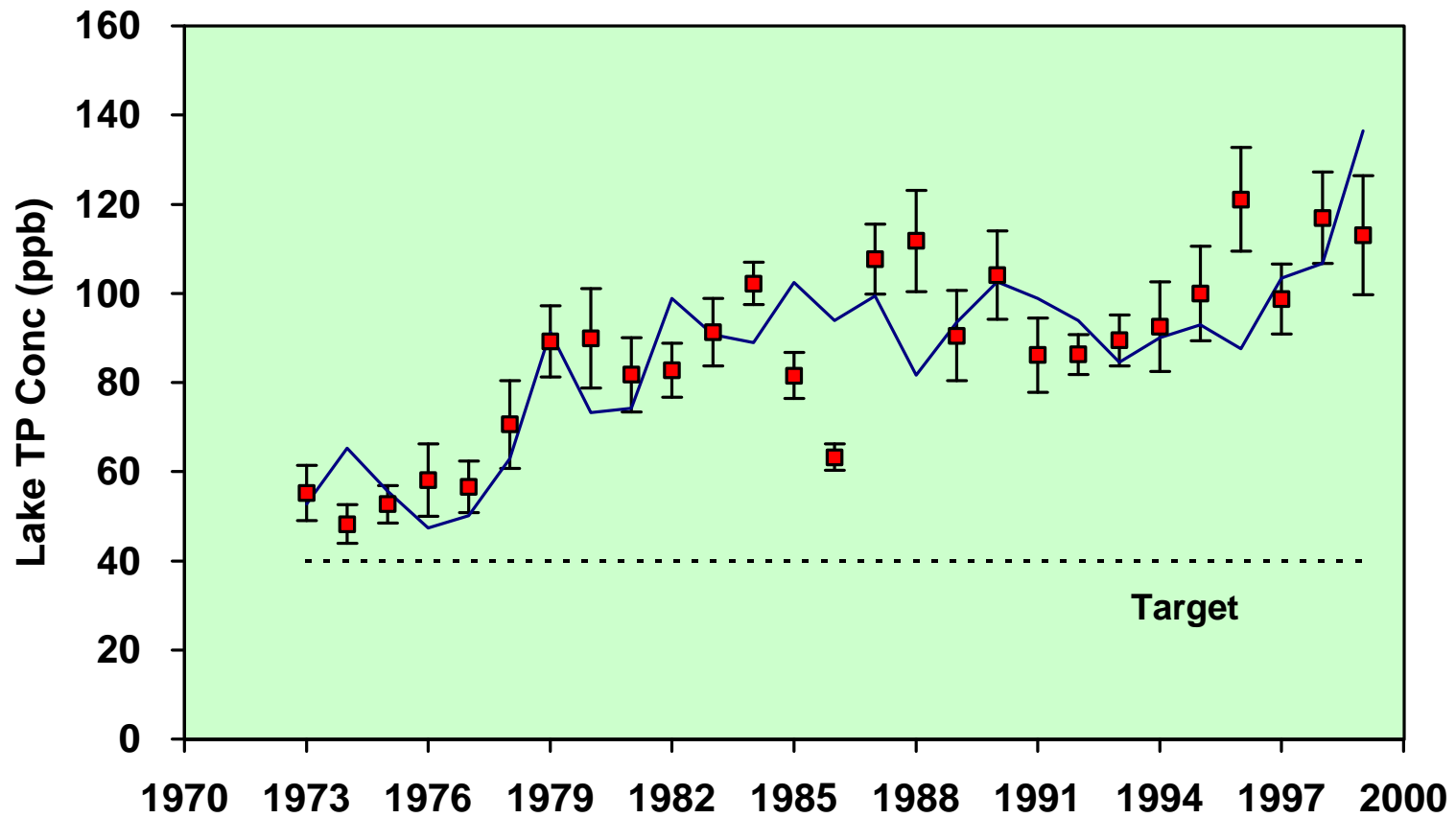
E: Maximum% of Measurements in Any 2-Week Period, All Seasons & Years (i.e., worst-case)

F: Lake Mean pH for June-July (Mean, Mean Yearly Maximum, 1/7 Year Maximum)

Figure 25
pH Simulations with Estimated Background Loads



Low, Best Estimate, High = Approximate 80% Confidence Interval for Estimated Background Inflow Concentration (55, 63, & 70 ppb)
 Corresponding to Reductions of 33%, 40%, & 47% in 1992-1998 Watershed P Loads



Mass Balance: $dM / dt = L - Q C - K_{NET} A C$

Phosphorus & Calcium Balances

P Fluxes in metric tons/yr

Period: 1973-1999 Ca Fluxes in 1000 metric tons/yr

